

# SCS 139

## II.4 Alternating Current

**Dr. Prapun Suksompong**

[prapun@siit.tu.ac.th](mailto:prapun@siit.tu.ac.th)

$$v_R = i_R R$$

$$i_C = C \frac{dv_C}{dt}$$

$$v_L = L \frac{di_L}{dt}$$



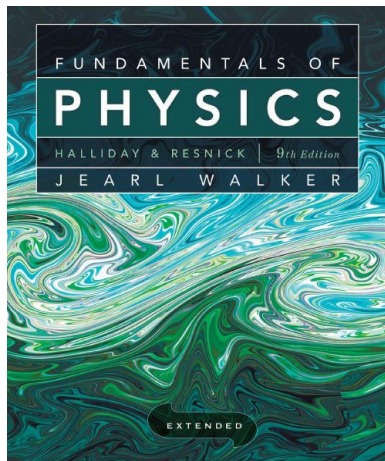
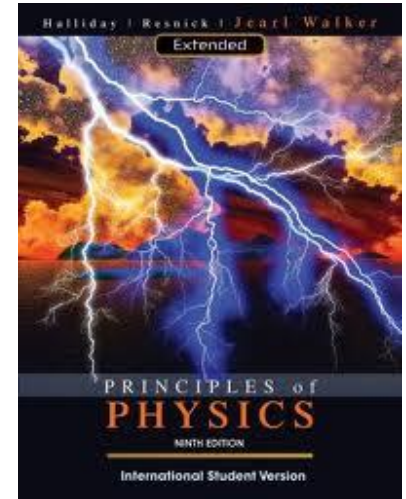
### Office Hours:

Library (Rangsit) Mon 16:20-16:50

BKD 3601-7 Wed 9:20-11:20

# Reference

- Principles of Physics
- Ninth Edition, International Student Version
- David Halliday, Robert Resnick,  
and Jearl Walker



- Chapter 31
  - 31-6 Alternating Current
  - 31-7 Forced Oscillations
  - 31-8 Three Simple Circuits

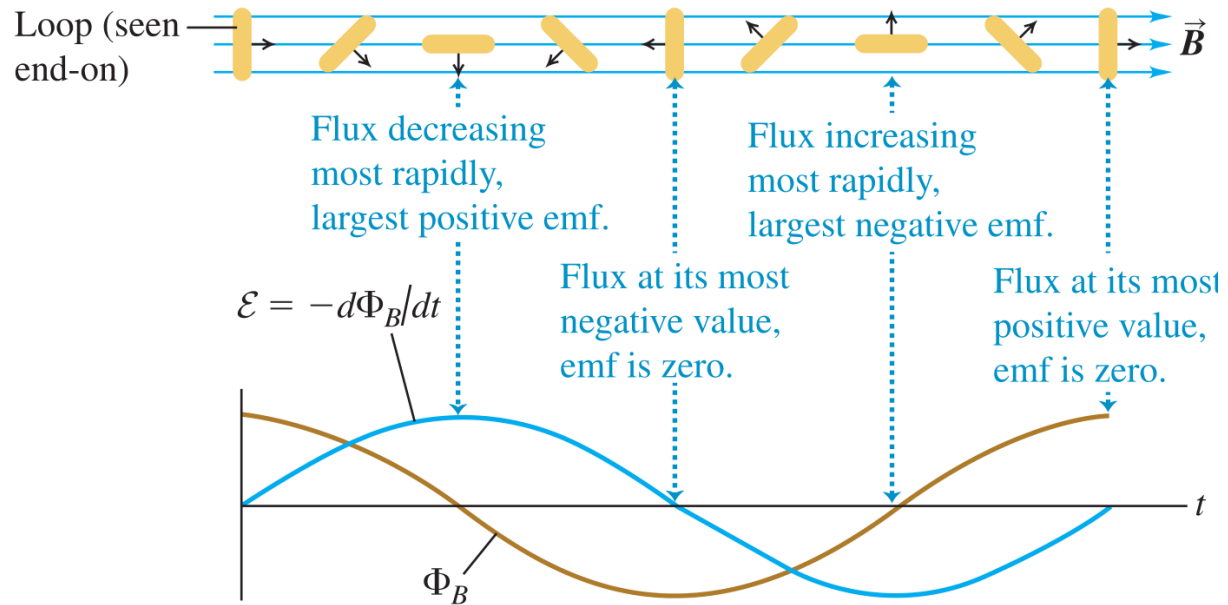
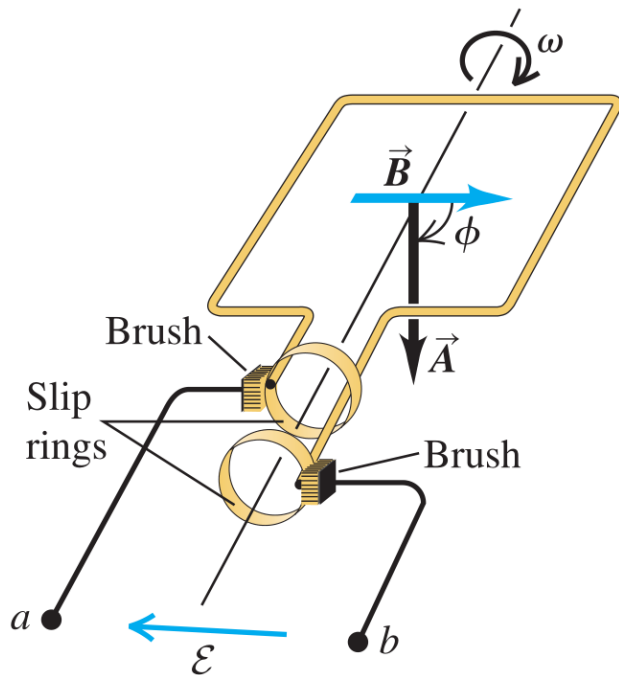
$$\Phi_B = BA \cos(\phi)$$

$$\phi = \omega t$$

# Alternating-Current Generator

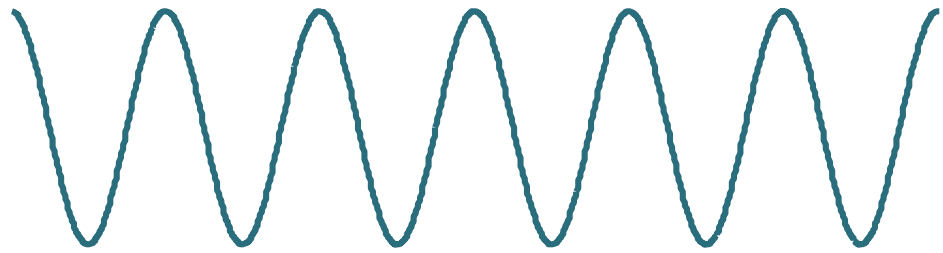
$$\mathcal{E}_{ind} = -N \frac{d\Phi_B}{dt} = BA(\sin \phi) \omega$$

- A conducting loop rotates (with constant angular speed  $\omega$ ) in an external (uniform and constant) magnetic field.

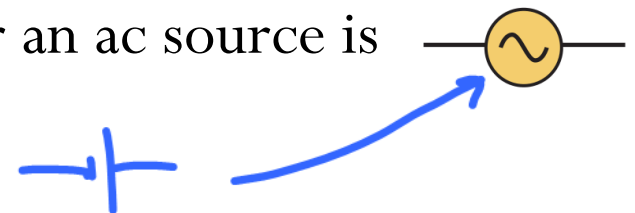


- Connections from each end of the loop to the external circuit are made by means of that end's slip ring.

# Sinusoids



- A **sinusoid** (or sinusoidal signal) is a signal (e.g. voltage or current) that has the form of the sine or cosine function.
  - Turn out that you can express them all under the same notation using only cosine (or only sine) function.
    - **We will use cosine.**
- A sinusoidal current is referred to as **alternating current** (ac).
- Circuits driven by sinusoidal (current or voltage) sources are called **ac circuits**.
  - We use the term **ac source** for any device that supplies a sinusoidally varying voltage (potential difference) or current
- The usual circuit-diagram symbol for an ac source is

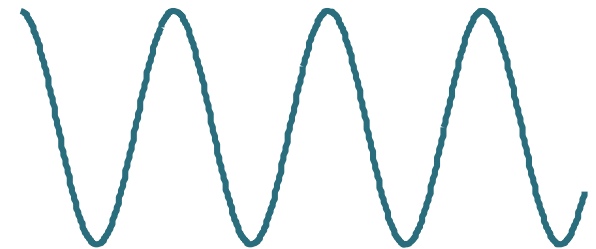


# Sinusoids: Standard Form

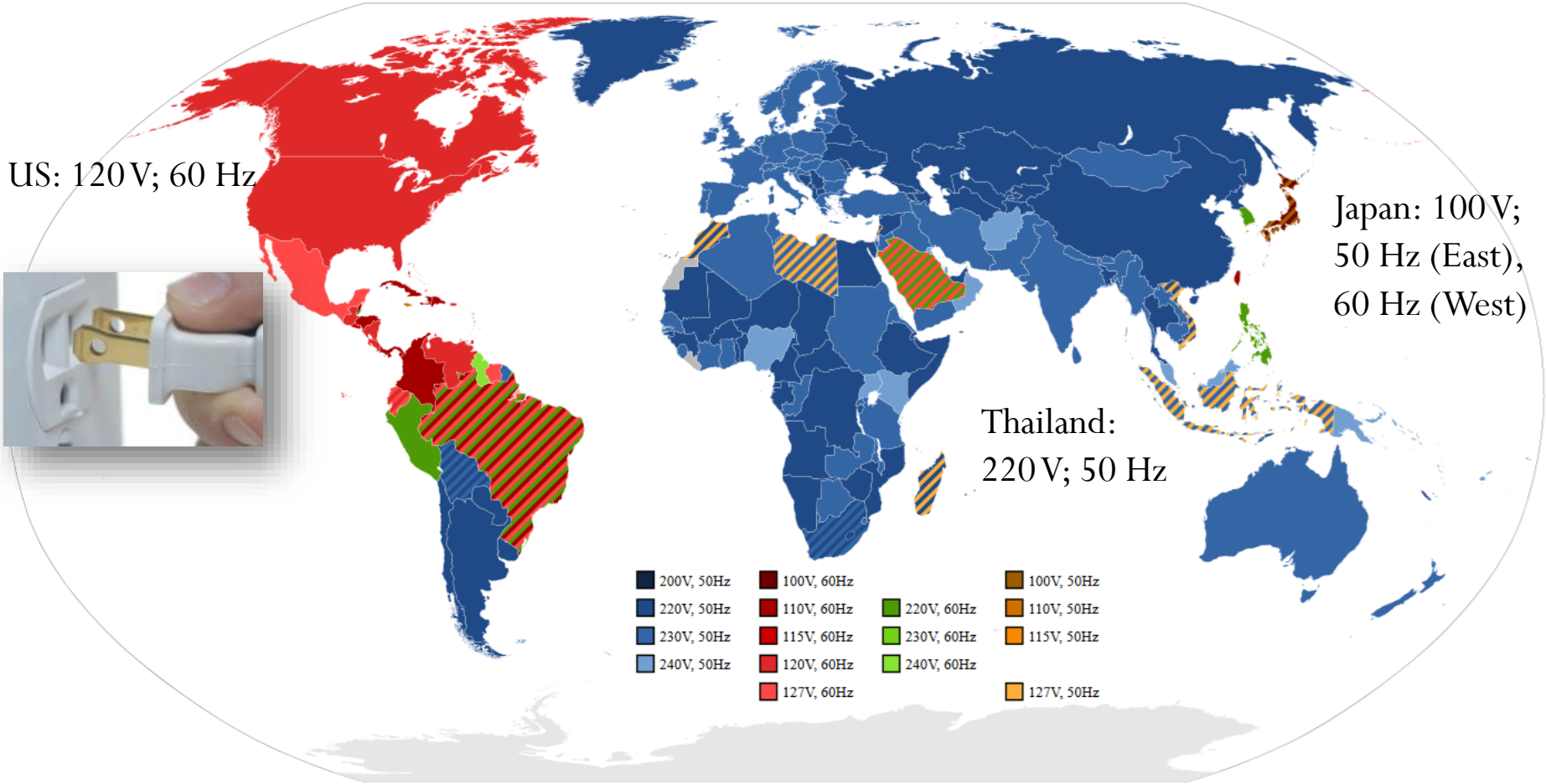
- General sinusoidal signal (in cosine form)

$$x(t) = X_m \cos(\omega t + \phi) = X_m \cos(2\pi f t + \phi).$$

- $X_m$ : amplitude of the sinusoid
  - Nonnegative when expressed in standard form
- $T$ : period (the time of one complete cycle)
- $f$ : frequency
  - #cycles per second or hertz (Hz)  $f = \frac{1}{T} = \frac{\omega}{2\pi}$
- $\omega$ : angular frequency in radians/s (or rad/s)
- $\phi$ : phase
  - Between  $-180^\circ$  and  $+180^\circ$  in standard form



# Around the World: Voltages and Frequencies



# Conversions to standard form

- When the signal is given in the sine form, it can be converted into its cosine form via the identity

$$\sin(x) = \cos(x - 90^\circ).$$

In particular,

$$X_m \sin(\omega t + \phi) = X_m \cos(\omega t + \phi - 90^\circ).$$

- We can avoid having  $X_m$  with negative sign by the following conversion:

$$-\cos(x) = \cos(x \pm 180^\circ).$$

In particular,

$$-A \cos(\omega t + \phi) = A \cos(2\pi ft + \phi \pm 180^\circ).$$

- Note that usually you do not have the choice between  $+180^\circ$  or  $-180^\circ$ . The one that you need to use is the one that makes  $\phi \pm 180^\circ$  falls somewhere between  $-180^\circ$  and  $+180^\circ$ .

# Exercise

Express the following sinusoids in their standard forms

$$5 \cos(2t - 45^\circ) = 5 \cos(2t + (-45^\circ))$$

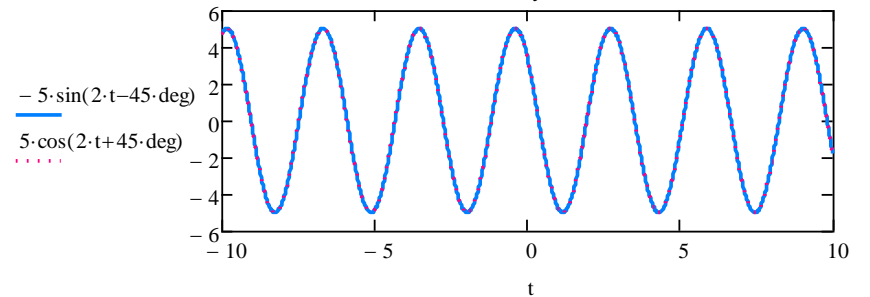
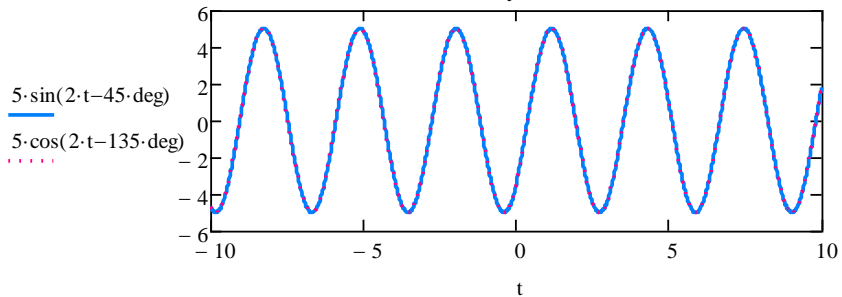
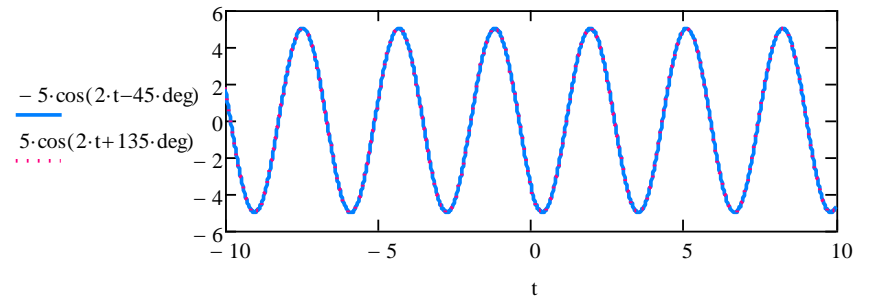
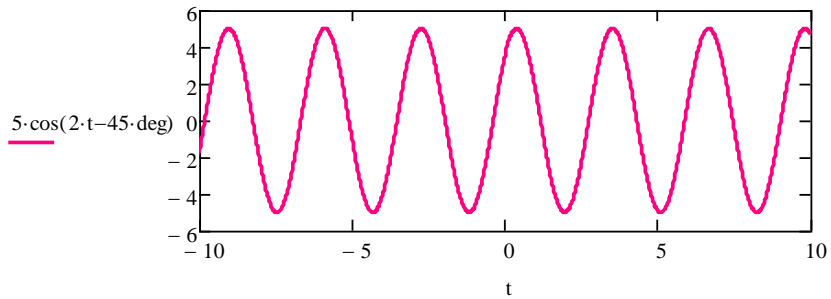
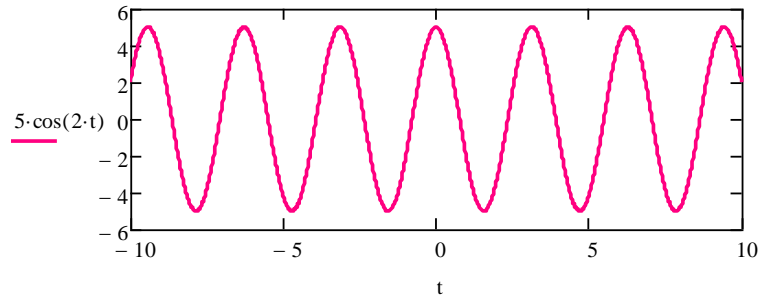
$$\begin{aligned} 5 \sin(2t - 45^\circ) &= 5 \cos(2t - 45^\circ - 90^\circ) \\ &= 5 \cos(2t + (-135^\circ)) \end{aligned}$$


$$\begin{aligned} -5 \cos(2t - 45^\circ) &= 5 \cos(2t - 45^\circ \oplus 180^\circ) \\ &= 5 \cos(2t + 135^\circ) \end{aligned}$$

$$\begin{aligned} -5 \sin(2t - 45^\circ) &= +5 \cos(2t - \underbrace{45^\circ - 90^\circ}_{-135^\circ} \oplus 180^\circ) \\ &= 5 \cos(2t + 45^\circ) \end{aligned}$$



# Exercise



$$i = I_m \cos(\omega t + \phi_i)$$



$$v = V_m \cos(\omega t + \phi_v)$$

$$v = iR$$

$$V_m \cos(\omega t + \phi_v) = I_m R \cos(\omega t + \phi_i)$$

$$V_m = I_m R$$

$$\phi_v = \phi_i$$

$$i = I_m \cos(\omega t + \phi_i)$$


$$v = V_m \cos(\omega t + \phi_v)$$

inductive reactance

$$V_m = (\omega L) I_m$$

$$\phi_v = \phi_i + 90^\circ$$

$$v = L \frac{di}{dt}$$

$$V_m \cos(\omega t + \phi_v) = L \omega I_m (-\sin(\omega t + \phi_i))$$

$$= \omega L I_m \cos(\omega t + \phi_i - 90^\circ \pm 180^\circ)$$

$$= \omega L I_m \cos(\omega t + \phi_i + 90^\circ)$$

# Application: Measuring Body Fat by Bioelectric Impedance Analysis

- The electrodes attached to this overweight patient's chest are applying a small ac voltage of frequency 50 kHz.
- The attached instrumentation measures the amplitude and phase angle of the resulting current through the patient's body.
- These depend on the relative amounts of water and fat along the path followed by the current, and so provide a sensitive measure of body composition.

